

1.

$$f(x) = x^3 + 3x^2 + 5.$$

Find

(a) $f''(x),$

(3)

(b) $\int_1^2 f(x) dx.$

(4)



9.

Figure 2

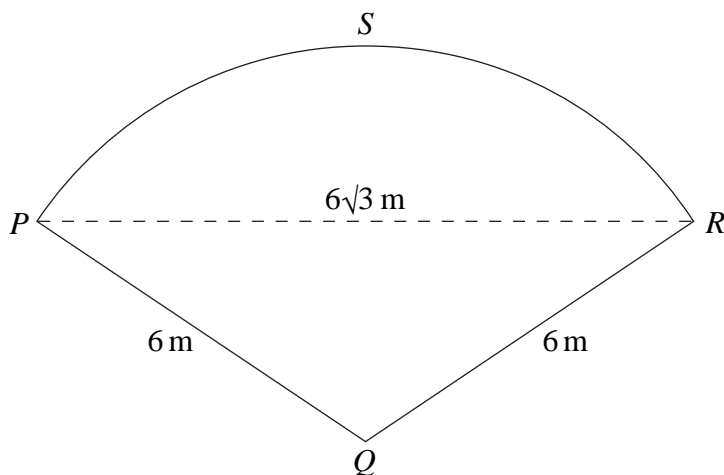


Figure 2 shows a plan of a patio. The patio $PQRS$ is in the shape of a sector of a circle with centre Q and radius 6 m .

Given that the length of the straight line PR is $6\sqrt{3}\text{ m}$,

- (a) find the exact size of angle PQR in radians. (3)
- (b) Show that the area of the patio $PQRS$ is $12\pi\text{ m}^2$. (2)
- (c) Find the exact area of the triangle PQR . (2)
- (d) Find, in m^2 to 1 decimal place, the area of the segment PRS . (2)
- (e) Find, in m to 1 decimal place, the perimeter of the patio $PQRS$. (2)



10. A geometric series is $a + ar + ar^2 + \dots$

(a) Prove that the sum of the first n terms of this series is given by

$$S_n = \frac{a(1-r^n)}{1-r}. \tag{4}$$

(b) Find

$$\sum_{k=1}^{10} 100(2^k). \tag{3}$$

(c) Find the sum to infinity of the geometric series

$$\frac{5}{6} + \frac{5}{18} + \frac{5}{54} + \dots \tag{3}$$

(d) State the condition for an infinite geometric series with common ratio r to be convergent.

(1)



